

VI SIMPOSIUM OF COMPUTER AIDED DESIGN AND ENGINEERING, BIOMECHANICS AND MECHATRONICS

Aeroelastic Behavior Of An Airfoil Typical Section Considering Nonlinear Unsteady Aerodynamics

Comportamiento Aeroelástico De Una Sección Típica De Un Perfil Aerodinámico Considerando Aerodinámica Inestable No Lineal

Luís F. M. S. Cassales¹, Lucas V. Caravita², Giovanne S. A. Silva³, Vagner C. Sousa⁴

1- Luís Felipe Moreira da Silva Cassales. Unesp, Brazil. E-mail: luis.cassales@unesp.br

2- Lucas Victorelli Caravita. Unesp, Brazil. E-mail: lucas.caravita@unesp.br

3- Giovanne Sooma Assunção Silva. Unesp, Brazil. E-mail: giovanne.sooma@unesp.br

4- Vagner Candido Sousa. Unesp, Brazil. E-mail: vagner.sousa@unesp.br

Abstract: This study compares simulation results for the aeroelastic behavior of an airfoil typical section by considering two distinct unsteady aerodynamics models: linear and nonlinear, for different airflow speeds. The considered aerodynamic models are the Edwards model, that treats the aerodynamic loading in a linear approximation, and the Beddoes-Leishman model, that treats the aerodynamic loading as a combination of linear and nonlinear contributions. The main goal of this study is to investigate the effects related to the dynamic stall phenomenon at airflow speeds above the linear critical flutter speed. As expected, simulation results show that the Beddoes-Leishman model represents the aeroelastic response of the airfoil more realistic, predicting the transformation of typical flutter unstable responses into stable limit-cycle oscillations at post-flutter airflow speeds.

Resumen: Este estudio compara los resultados de la simulación para el comportamiento aeroelástico de una sección típica de un perfil aerodinámico considerando dos modelos aerodinámicos inestables distintos: lineal y no lineal, para

1

diferentes velocidades de flujo de aire. Los modelos aerodinámicos considerados son el modelo de Edwards, que trata la carga aerodinámica en una aproximación lineal, y el modelo de Beddoes-Leishman, que trata la carga aerodinámica como una combinación de contribuciones lineales y no lineales. El objetivo principal de este estudio es investigar los efectos relacionados con el fenómeno de pérdida de sustentación dinámica a velocidades de flujo de aire superiores a la velocidad de aleteo crítica lineal. Como se esperaba, los resultados de la simulación muestran que el modelo Beddoes-Leishman representa la respuesta aeroelástica del perfil aerodinámico de manera más realista, prediciendo la transformación de respuestas inestables típicas de aleteo en oscilaciones estables de ciclo límite a velocidades de flujo de aire posteriores al aleteo.

Keywords: Aeroelasticity; Nonlinear Aerodynamics; Flutter; Dynamic Stall.

Palabras Claves: Aerolasticidade; Aerodiámica Non Lineal; Aleteo; Pérdida de Sustentación Dinámica.

1. Introduction

In aeronautical sector, a particularly aeroelastic phenomenon of interest is the flutter, due to its catastrophic potential, being involved in several aeronautical accidents.

 Flutter is considered as a dynamic instability, which manifests from a certain flow speed, considered the critical system parameter. Briefly, flutter can be understood as being: stable for speeds below the critical speed, marginally stable at the critical speed and unstable for speeds above the critical speed, where self-sustained oscillations appear. The arise of these self-sustained oscillations is the reason for the catastrophic nature of flutter, since, physically, this denotes into displacements of increasing amplitudes, until the collapse of the structure [1].

 For linear aerodynamic models, the typical flutter behavior discussed above is expected. However, under specific conditions, nonlinearities can be added to the system, so that self-sustaining oscillations of increasing amplitude are replaced by limit-

cycle oscillations (LCOs) of constant amplitude [2]. A source of non-linearity are the effects arising from the dynamic stall, which results from the loss of lift forces on the airfoil, due to the separation of the flow [1].

 This study aims to compare the response of an aeroelastic system when two different aerodynamic models are used: one of them is the Edwards model, which represents a linear aerodynamics, and the other is the Beddoes-Leishman (BL) model, which represents a non-linear aerodynamics.

2. Methodology

 The methodology consisted of a literature review and computer simulation of the models, as it follows on the next sections.

2.1 Beddoes-Leishman Model

 The BL model was initially proposed through the use of indicial functions [3], and later adapted to a state-space representation [4]. The state-space representation was chosen due to its relative ease of implementation.

 To represent BL aerodynamics model, there is a system of 12 states ODEs, being: 8 corresponding to the linear portion of the flow, 3 referring to the progressive detachment of the flow at the trailing edge (non-linear phenomenon) and the remaining state corresponds to the dynamic stall process. The states referring to the linear portion are presented in Equations (2.1.1) and (2.1.2).

$$
\{\dot{x}\} = [A]\{x\} + [B]\begin{Bmatrix} \alpha \\ q \end{Bmatrix} \tag{2.1.1}
$$

$$
\begin{Bmatrix} C_N^p \\ C_M^p \end{Bmatrix} = [C]\{x\} + [D]\begin{Bmatrix} \alpha \\ q \end{Bmatrix}
$$
\n(2.1.2)

 Matrices A, B, C and D are dependent on semi-empirical constants of the model and flow speed [4]. The terms α and q (angle of attack and pitch rate, respectively), are inputs related to the structural part of the problem. Using the response of the linear part of the problem, it is possible to determine the effective angle of attack (α_F) , given by Equation (2.1.3), this term is related to the viscous effects on the airfoil.

$$
\alpha_E(t) = \beta^2 \left(\frac{2V_\infty}{c}\right) (A_1 x_1 b_1 + A_2 x_2 b_2)
$$
\n(2.1.3)

The first non-linear state is related to the stall. In [5] corrections are proposed taking into account non-stationary conditions for the stall model based on the critical pressure on the leading edge [6]. Thus, the pressure is associated with aerodynamic normal forces (C_N) , as well as with a delay due to the non-stationary part (C'_N) .

$$
\dot{x}_{9} = \left(\frac{2V_{\infty}}{c}\right) \frac{-x_{9} + C_{N}^{p}(t)}{T_{P}}
$$
\n(2.1.4)

$$
x_9 = C'_N(t) \tag{2.1.5}
$$

In Equation (2.1.4), the term $(2V_{\infty}/c)$ is a constant that makes the equation dimensional, and $C_N^P(t)$ is the value obtained by Equation (2.1.2) and T_P a constant of time. The value obtained through Equation (2.1.5) is used to determine the condition of the flow, if $|C_N| \ge C_{N_1}$ there will be detachment of the flow, where C_{N_1} is the critical value for the normal force under static conditions, and after the detachment of the flow there will be the reattachment when $|C'_N| < C_{N_1}$.

 The next two states are related to aerodynamic loads derived from the Kirchhoff model for a flat plate, and represent flow separation and vortex detachment at the trailing edge of the profile. To find the point where the flow separation occurs, it is necessary to determine an equivalent angle of attack (α_F) [7], which takes into account the non-linear effects and finds an equivalent angle for the static case that would result in the same pressure on the leading edge, thus using the term given by Equation (2.1.5) and the slope of the normal force curve $(C_{N_{\alpha}})$, we have Equation (2.1.6).

$$
\alpha_F = \frac{C_N'}{C_{N_\alpha}}\tag{2.1.6}
$$

Using α_F , the position of the flow separation is determined from Equation (2.1.7). Where the terms s_1 and s_2 are empirical coefficients, and α_1 the static stall angle, considered for a value of $f = 0.7$ in most airfoils. The values adopted were taken from references [8] and [9].

$$
f(\hat{\alpha}) = \begin{cases} 1 - 0.3e^{\frac{|\hat{\alpha}| - \alpha_1}{S_1}} & \text{if } |\hat{\alpha}| \le \alpha_1 \\ 0.04 - 0.66e^{\frac{\alpha_1 - |\hat{\alpha}|}{S_2}} & \text{if } |\hat{\alpha}| > \alpha_1 \end{cases}
$$
(2.1.7)

$$
\dot{x}_{10} = \left(\frac{2V_{\infty}}{c}\right) \frac{-x_{10} + f(\alpha_F)}{T_f} \tag{2.1.8}
$$

$$
x_{10} = f''(t) \tag{2.1.9}
$$

The term $f''(t)$ corresponds to flow separation due to delays, and T_f varies according to the flow conditions discussed for C_N' . For the vortex detachment condition T_f is given by the conditions presented in Equation (2.1.10).

$$
T_f = \begin{cases} T_{f0} \text{ if } 0 \le \tau_v \le T_{vl} \text{ and } \alpha \dot{\alpha} \ge 0 \\ \frac{1}{3} T_{f0} \text{ if } T_{vl} < \tau_v \le 2T_{vl} \text{ and } \alpha \dot{\alpha} \ge 0 \\ \frac{1}{2} T_{f0} \text{ if } 0 \le \tau_v \le T_{vl} \text{ and } \alpha \dot{\alpha} < 0 \\ 4T_{f0} \text{ if } 2T_{vl} < \tau_v \end{cases} \tag{2.1.10}
$$

 T_{f0} and T_{vl} are empirical parameters and $\tau_v = 2V_{\infty}/c$ a counter that runs with dimensionless time. During this phase, there is a change in α_1 , with increments dependent on a $\delta_{\alpha 1}$, according to Equation (2.1.11).

$$
\alpha_1 = \begin{cases} \alpha_{1_0} & \text{if } \alpha \dot{\alpha} \ge 0 \\ \alpha_{1_0} - \left(1 - \alpha_{1_0}\right)^{0.25} \delta_{\alpha 1} & \text{if } \alpha \dot{\alpha} < 0 \end{cases} \tag{2.1.11}
$$

After the flow reattachment, T_f is given by Equation (2.1.12), and the value of α_1 returns to being the critical angle for the static case.

$$
T_f = \begin{cases} T_{f0} & \text{if } f'' \ge 0.7\\ 2T_{f0} & \text{if } f'' < 0.7 \end{cases} \tag{2.1.12}
$$

4th International Scientific Convention UCLV 2023 Central University "Marta Abreu" of Las Villas "AEROELASTIC BEHAVIOR OF AN AIRFOIL TYPICAL SECTION CONSIDERING NONLINEAR UNSTEADY AERODYNAMICS"

$$
\alpha_1 = \alpha_{1_0} \tag{2.1.13}
$$

 The next state comes from a change in the Kirchhoff model for the pitch moment in the vortex shedding region [10]. Where the f_m term of Equation (2.1.15) is similar to the term described by Equation (2.1.9).

$$
\dot{x}_{11} = \left(\frac{2V_{\infty}}{c}\right) \frac{2\left(-x_{11} + f(\alpha_F)\right)}{T_{f0}}\tag{2.1.14}
$$

$$
x_{11} = f_m(t) \tag{2.1.15}
$$

 From the terms obtained previously, the aerodynamic loads can be given by the expressions presented in Equation (2.1.16).

$$
\begin{cases}\nC_N^f(t) = C_N^c(t) \left(\frac{1 + \sqrt{f''}}{2}\right)^2 \\
C_M^f(t) = C_N^c(t) \{K_0 + K_1(1 - f) + K_2 \sin(\pi f^2)\} + C_{M_0} \\
C_T^f(t) = \eta C_{N_\alpha} \sqrt{f''} \left(\frac{C_N^c}{C_{N_\alpha}}\right)^2\n\end{cases}
$$
\n(2.1.16)

 K_0, K_1 and K_2 are empirical values, \hat{f} the greater value between x_{10} and x_{11} , and $C_N^c = C_{N_\alpha} \alpha_E$. The last state refers to dynamic stall. Before the flow detachment, the characteristic vortices are neglected. After the detachment condition is reached the behavior will be given by Equation (2.1.17) and Equation (2.1.18).

$$
\dot{x}_{12} = \left(\frac{2V_{\infty}}{c}\right) \frac{-x_{12} + \dot{C}_v}{T_v} \tag{2.1.17}
$$

$$
x_{12} = C_N^{\nu}(t) \tag{2.1.18}
$$

Empirical terms (T_{v0} and T_{vl}) and the counter τ_v are used for the calculation of the term T_v , described in Equation (2.1.19).

4th International Scientific Convention UCLV 2023 Central University "Marta Abreu" of Las Villas "AEROELASTIC BEHAVIOR OF AN AIRFOIL TYPICAL SECTION CONSIDERING NONLINEAR UNSTEADY AERODYNAMICS"

$$
T_v = \begin{cases} T_{v0} \text{ if } 0 \le \tau_v \le T_{vl} \text{ and } \alpha \dot{\alpha} \ge 0 \\ 0.25T_{v0} \text{ if } T_{vl} < \tau_v \le 2T_{vl} \text{ and } \alpha \dot{\alpha} \ge 0 \\ 0.5T_{v0} \text{ if } 0 \le \tau_v \le T_{vl} \text{ and } \alpha \dot{\alpha} < 0 \\ 0.9T_{v0} \text{ if } 2T_{vl} < \tau_v \end{cases} \tag{2.1.19}
$$

 The normal force coefficient is determined by Equation (2.1.20) and the moment coefficient by Equation $(2.1.21)$.

$$
C_v = \begin{cases} C_N^c \left[1 - 0.25 \left(1 + \sqrt{f''} \right)^2 \right] & \text{if } \tau_v \le 2T_{vl} \\ 0 & \text{if } \tau_v > 2T_{vl} \end{cases} \tag{2.1.20}
$$

$$
C_M^{\nu}(t) = -0.25 \left[1 - \cos\left(\frac{\pi \tau_{\nu}}{T_{\nu l}}\right) \right] C_n^{\nu} \tag{2.1.21}
$$

Thus, the final aerodynamic response will be given by Equation (2.1.22) and (2.1.23).

$$
C_{m_{ra}}(t) = C_M^p(t) + C_M^f(t) + C_m^v(t) + [C_N^p(t) - C_N^c(t) + C_N^f(t) + C_N^v(t)](X_{ea} - X_{ac}) \tag{2.1.22}
$$

$$
C_l(t) = \left[C_N^p(t) - C_N^c(t) + C_N^f(t) + C_N^v(t)\right] \cos\alpha(t) - C_T^f(t) \sin\alpha(t) \tag{2.1.23}
$$

2.2 Structural Model

 The structural model uses a typical section with 2-DOF, as described by Figure 2.2.1. The dimensionless state space representation for the structural part is given in Equation (2.2.1).

$$
\begin{bmatrix} \mu & x_{\theta} \\ x_{\theta} & r_{\theta}^2 \end{bmatrix} \begin{Bmatrix} \ddot{h}(t) \\ \ddot{\theta}(t) \end{Bmatrix} + \begin{bmatrix} \zeta_h & 0 \\ 0 & \zeta_{\theta} \end{bmatrix} \begin{Bmatrix} \dot{h}(t) \\ \dot{\theta}(t) \end{Bmatrix} + \begin{bmatrix} 1 & 0 \\ 0 & n_{\theta}^2 r_{\theta}^2 \end{bmatrix} \begin{Bmatrix} \dot{h}(t) \\ \theta(t) \end{Bmatrix} = \begin{Bmatrix} -\dot{L} \\ \dot{M}_{\theta} \end{Bmatrix}
$$
(2.2.1)

Figure 1. Typical aeroelastic section [9].

7

Where μ is the ratio of the airfoil mass to the total mass, η_{θ} is the frequency ratio, r_{θ} is the dimensionless gyration radius, x_{θ} is the dimensionless distance between the elastic center and the CG, and ζ_h and ζ_θ are damping ratios [11]. Using the values for the angle of attack (α) and the pitch rate (q) , together with Equation (2.2.2), the inputs for the BL model can be determined.

$$
\begin{cases}\n\alpha(t) = \theta(t) + \arctan\left[\frac{\dot{h}(t)}{V_{\infty}}\right] & (2.2.2) \\
q(t) = \left(\frac{c}{V_{\infty}}\right)\dot{\theta}(t)\n\end{cases}
$$

2.3 Edwards Model

 The Edwards model also uses, according to [12] a state space matrix for the structural part, which can be seen in Equation (2.3.1), and in Equation (2.3.2 and 2.3.3), for lift and aerodynamic moment, where, as in the case of Beddoes-Leishman, the structural part uses the aerodynamic output as input and vice versa.

$$
\begin{bmatrix} I & 0 \\ 0 & M \end{bmatrix} \begin{bmatrix} \dot{x}_s \\ \ddot{x}_s \end{bmatrix} + \begin{bmatrix} 0 & -I \\ K & B \end{bmatrix} \begin{bmatrix} x_s \\ \dot{x}_s \end{bmatrix} = \begin{bmatrix} 0 \\ F \end{bmatrix}
$$
 (2.3.1)

$$
M_{\alpha} = -\rho b^2 \left[\pi \left(\frac{1}{2} - a \right) U b \dot{\alpha} + \pi b^2 \left(\frac{1}{8} + a^2 \right) \ddot{\alpha} - \dot{\alpha} \pi b \ddot{h} \right] + 2\rho U b^2 \pi \left(a + \frac{1}{2} \right) C_{(K)} f_{(t)} \tag{2.3.2}
$$

$$
L = -\rho b^2 \left(U\pi \dot{\alpha} + \pi \ddot{h} - \pi b a \ddot{\alpha} \right) - 2\pi \rho U b C_{(K)} f_{(t)} \tag{2.3.3}
$$

Where x_s is a 2x1 matrix that contains the angle of attack α and the translation parameter h. The F parameter is also a 2x1 matrix that contains the values, respectively, of aerodynamic moment and lift. The terms M, K and B represent the mass, suffering and damping without the non-circulating contributions of the airfoil. In the case of the Edwards model, however, it is possible to couple the structural and aerodynamic equations, where with some manipulations described in [12] we arrive at the following coupled state space, Equation (2.3.4).

$$
\begin{bmatrix} I & 0 & 0 \\ 0 & \dot{M} & 0 \\ 0 & 0 & \dot{I} \end{bmatrix} \begin{bmatrix} \dot{x}_s \\ \dot{x}_s \\ \dot{x}_a \end{bmatrix} = \begin{bmatrix} 0 & I & 0 \\ \dot{K} & \dot{B} & \dot{D} \\ \dot{E}_1 & \dot{E}_2 & \dot{F}_P \end{bmatrix} \begin{bmatrix} x_s \\ \dot{x}_s \\ x_a \end{bmatrix} \tag{2.3.4}
$$

The terms \mathbf{F}_1 and \mathbf{F}_2 represent first order equations of the aerodynamic model and \hat{D} a dimensioless time. These terms are demonstrated in Equations (2.3.5, 2.3.6 and 2.3.7).

$$
\mathcal{E}_1 = \left(\frac{1}{\omega_h}\right)^2 \left(\frac{U}{b}\right) \begin{bmatrix} 0\\ S_1 \end{bmatrix} \tag{2.3.5}
$$

$$
\mathcal{E}_2 = \frac{1}{\omega_h} \begin{bmatrix} 0 \\ S_2 \end{bmatrix} \tag{2.3.6}
$$

$$
B = \frac{1}{\omega_h^2} D \tag{2.3.7}
$$

The terms *(mass term),* $*K*$ *(stiffness term) and* $*B*$ *(damping term) are* expressed in Equations (2.3.8, 2.3.9 and 2.3.10).

$$
M = M - \frac{\rho b^2}{m} M_{nc}
$$
 (2.3.8)

$$
K = K - \frac{\rho b^2}{m} \left(\frac{U}{\omega_h b}\right)^2 \left(K_{nc} + \frac{1}{2} R S_1\right)
$$
 (2.3.9)

$$
B = B - \frac{\rho b^2}{m} \left(\frac{U}{\omega_h b}\right) \left(B_{nc} + \frac{1}{2} R S_2\right)
$$
 (2.3.10)

The terms M_{nc} , K_{nc} and B_{nc} represent non-circulatory contributions from mass, shaking and damping respectively. The configurations R, S_1 , S_2 and S_3 are vectors related to the circulatory part of the system, the part that corresponds to the noncirculatory terms can be seen in Equations (2.3.11, 2.3.12 and 2.3.13).

$$
M_{nc} = \begin{bmatrix} -\pi \left(\frac{1}{8} + a^2\right) & -2T_{13} & \pi a \\ -2T_{13} & \frac{T_3}{\pi} & T_1 \\ \pi a & T_1 & -\pi \end{bmatrix}
$$
(2.3.11)

$$
K_{nc} = \begin{bmatrix} 0 & -(T_{10} + T_4) & 0 \\ 0 & \frac{1}{\pi} (T_4 T_{10} - T_5) & 0 \\ 0 & 0 & 0 \end{bmatrix}
$$
(2.3.12)

$$
B_{nc} = \begin{bmatrix} \pi \left(a - \frac{1}{2} \right) & 2\rho + \left(\frac{1}{2} - a \right) T_4 & 0 \\ -\rho + T_1 + \frac{T_4}{2} & \frac{T_{11} T_4}{2\pi} & 0 \\ -\pi & T_4 & 0 \end{bmatrix}
$$
(2.3.13)

 The vectors corresponding to the circulatory system are shown in Equation (2.3.14, 2.3.15, 2.3.16 and 2.3.17).

$$
R = \begin{bmatrix} 2\pi \left(a + \frac{1}{2} \right) \\ -T_{12} \\ -2\pi \end{bmatrix}
$$
 (2.3.14)

$$
S_1 = \begin{bmatrix} 1 & \frac{T_{10}}{\pi} & 0 \end{bmatrix} \tag{2.3.15}
$$

$$
S_2 = \left[\left(\frac{1}{2} - a \right) \frac{T_{11}}{2\pi} \quad 1 \right] \tag{2.3.16}
$$

$$
S_3 = \left[0.006825 \left(\frac{U}{b}\right)^2 \quad 0.10805 \left(\frac{U}{b}\right)\right] \tag{2.3.17}
$$

 In the aerodynamic equations (2.3.2 and 2.3.3) there is the presence of the factor $C_{(k)}f_{(t)}$, which is composed of the multiplication of the Theodorsen function $(c_{(k)}f_{(t)})$ by the term $f_{(t)}$. The term is obtained through Equation (2.3.18).

$$
f_{(t)} = U\alpha + \dot{h} + b\left(\frac{1}{2} - a\right)\dot{\alpha} \tag{2.3.18}
$$

 However, through manipulations and approximations [12] the multiplication $C_{(k)} f_{(t)}$ can be replaced by Equation (2.3.19).

$$
C_{(k)}f_{(t)} = (C_0 + C_1 + C_2)f_{(t)} + C_3C_4(C_1 + C_2)x_{a1} + (C_1C_3 + C_2C_4)x_{a2}
$$
 (2.3.19)

Where the terms x_{a1} and x_{a2} are included, which together make up a 2x1 matrix that is part of eq. 2.3.4 ($x_a = [x_{a1} x_{a2}]^T$), in addition the terms of Equation (2.3.19) that multiply these two parameters are represented in dimensionless form in Equation (2.3.4) through the parameter F_p , demonstrated in Equation (2.3.20).

$$
\bar{F}_P = \frac{1}{\omega_h} \begin{bmatrix} 0 & 1 \\ -0.01365 \left(\frac{U}{b}\right)^2 & -0.3455 \left(\frac{U}{b}\right) \end{bmatrix}
$$
(2.3.20)

The values from T_1 to T_{14} are known as Theodorsen constants and can be found in [12].

3. Results and Discussion

 The results obtained through the Edwards and BL models were compared for speeds greater than and equal to the critical speed (the parameters used were the same as used in [8]). In this case, the V_{cr} found is 14.49 m/s.

 Also has been made the comparison between the BL model with the influence of nonlinear parameters and without this influence, the results obtained can be verified through the graphs of θ, h and α, where the first two represent elastic deformations in the airfoil section and the third the angle of attack, determined through the structural equation (2.3.2).

 The Fig. 2 shows the results of the models for the critical speed 14.49 m/s, where the amplitudes of the angle of attack, rotation and translation remain constant. The results are very similar between the models, with little variation in amplitude, so both models still provide reliable results at the critical speed.

Figure 2. Flutter critical speed [own elaboration].

 At speeds above flutter speed, where a dynamic stall occurs, the difference between the models is noticed. Fig. 3 shows the impact for a speed of 17 m/s, where the BL model reaches a value limit amplitude, which was already expected, due to the effect of the non-linearities generated by the dynamic stall. In the Edwards model, the movements continue to increase in amplitude even after the angle at which the dynamic stall would theoretically occur, since this model does not consider this type of nonlinearity.

 The differences between the models for high angles of attack is what differentiates them and defines the BL model as much closer to reality in this case. It is also notable that there is a difference in the amplitude of the two models before dynamic stall, where the BL model has larger angles.

Figure 3. Speeds above the critical speed of flutter [own elaboration].

 When compared, the BL model shows the great difference between considering or not the non-linearities, since from the critical speed there is a very large increase in the amplitude when the effect of the dynamic stall is not considered, making clear the need to consider it when working in this speed range.

Figure 4. Comparison between linear and non-linear Beddoes-Leishman [own elaboration].

4th International Scientific Convention UCLV 2023 Central University "Marta Abreu" of Las Villas "AEROELASTIC BEHAVIOR OF AN AIRFOIL TYPICAL SECTION CONSIDERING NONLINEAR UNSTEADY AERODYNAMICS"

4. Conclusions

Two different situations were compared between BL and Edwards methods: the airfoil response for the above cases and the critical flutter speed. The predicted linear flutter speed for the airfoil is 14.49 m/s. At this speed, the models predict comparable amplitude and frequency. By increasing the speed to 17.0 m/s the amplitude of the models varies. The Edwards model continues to have its amplitude increased continuously while the BL model tends to stabilize at a point.

 These results can be explained by the dynamic stall, that decreases the aerodynamic forces at high angles due to detachment of the boundary layer, causing the structural forces to stand out and tend to maintain a maximum and constant range of motion. The results are important to show that the BL model is capable of simulating in a more realistic way the behavior of the airfoil in a case above the flutter speed, being more suitable for simulating events that will occur in this speed range.

 The BL model implemented in this work could be used to analyze the total energy harvested by using a piezoelectrical coupling in an airfoil typical section made in laboratory during a dynamical stall condition as a continuation of this work.

5. Bibliographic references

- [1] DIMITRIADIS, G.; LI, J. Bifurcation behavior of airfoil undergoing stall flutter oscillations in low-speed wind tunnel. AIAA Journal, AIAA, v. 47, n. 11, p. 2577–2596, 2009.
- [2] DOWELL, E. H.; EDWARDS, J.; STRAGNAC, T. W. Nonlinear Aeroelasticity. Journal of Aircraft, AIAA, v. 40, n. 5, p. 857–874, 2003.
- [3] LEISHMAN, J. G.; BEDDOES, T. S. A semi-empirical model for dynamic stall. Journal of the American Helicopter Society, v. 34, p. 3–17, 1989.
- [4] LEISHMAN, J. G.; CROUSE, G. State-space models for unsteady airfoil behavior and dynamic stall. 30th Structures, Structural Dynamics and Materials Conference, AIAA 89-1319, p. 1372–1383, 1989.
- [5] Beddoes, T.S. Onset of Leading Edge Separation Effects Under Dynamic Conditions and Low Mach Number, Proceedings of the 34th Annual Forum of the American Helicopter Society, 1978.
- [6] EVANS, W. T.; MORT, K. W. Analysis of computed flow parameters for a set of sudden stalls in low-speed two- dimensional flow. NASA Technical Note, n. D-85, 1959.

- [7] CHANTHARASENAWONG, C. Nonlinear Aeroelastic Behaviour of Aerofoils Under Dynamic Stall. PhD Thesis - University of London, South Kensington, London - UK, 2007.
- [8] SANTOS, C. R. dos; PEREIRA, D. A.; MARQUES, F. D. On limit cycle oscillations of typical aeroelastic section with different preset angles of incidence at low airspeeds. Journal of Fluids and Structures, ELSEVIER, v. 74, p. 19–34, 2017.
- [9] SANTOS, C. R. dos; MARQUES, F. D.; HAJJ, M. R. The effects of structural and aerodynamic nonlinearities on the energy harvesting from airfoil stallinduced oscillations. Journal of Vibration and Control, SAGE, v. 25, n. 14, p. 1991–2007, 2019.
- [10]LEISHMAN, J. G.; BEDDOES, T. S. A generalized model for airfoil unsteady aerodynamic behavior and dynamic stall using indicial method. 42nd Annual Forum of the American Helicopter Society, 1986.
- [11] SOUSA, V. C.; MARQUI, C. J. de. Effect of pseudoelastic hysteresis of shape memory alloy springs on the aeroelastic behavior of a typical airfoil section. Journal of Intelligent Material Systems and Structures, SAGE, v. 27, n. 1, p. 117–133, 2014.
- [12] SOUSA, V.; Effects of superelastic shape memory springs on the aeroelastic behavior of a typical airfoil section: passive vibration attenuation and energy harvestig applications. PhD Thesis. Sao Carlos, Brazil, 2016.